Maths Calculation Policy

Isamilo International School Mwanza





IISM Calculation Policy – January 2020

<u>Concrete – Pictorial - Abstract</u>

What is the Concrete Pictorial Abstract approach in Maths?

The Concrete Pictorial Abstract (CPA) approach is a system of learning that uses physical and visual aids to build a child's understanding of abstract topics. Pupils are introduced to a new mathematical concept through the use of **concrete** resources (e.g. fruit, Dienes blocks etc).

When they are comfortable solving problems with physical aids, they are given problems with pictures – usually **pictorial representations** of the concrete objects they were using.

Then they are asked to solve problems where they only have the **abstract** i.e. numbers or other symbols. Building these steps across a lesson can help pupils better understand the relationship between numbers and the real world, and therefore helps secure their understanding of the mathematical concept they are learning.

Why use the Concrete Pictorial Abstract approach in Maths?

Pupils achieve a much deeper understanding if they don't have to resort to rote learning and are able to solve problems without having to memorise. When teaching reading to young children, we accept that children need to have seen what the word is to understand it. Putting together the letters c- a- t would be meaningless and abstract if children had no idea what a cat was or had never seen a picture.

People often don't think of this when it comes to maths, but to children many mathematical concepts can be equally meaningless without a concrete resource or picture to go with it. This applies equally to mathematics teaching at Early Years, KS1 or at KS2.

Effective use of the Concrete Pictorial Abstract method.

A common misconception with this CPA model is that you teach the concrete, then the pictorial and finally the abstract. But all stages should be taught simultaneously whenever a new concept is introduced and when the teacher wants to build further on the concept. When concrete resources, pictorial representations and abstract recordings are all used within the same activity, it ensures pupils are able to make strong links between each stage.

[https://thirdspacelearning.com/blog/concrete-pictorial-abstract-maths-cpa/]



Calculation Policy: Addition

Key Vocabulary - sum, total, parts and wholes, plus, add, altogether, more, 'is equal to' 'is the same as'.

Concrete	Pictorial	Abstract
Combining two parts to make a whole (use other resources too e.g. eggs, shells, teddy bears, cars).	Children to represent the cubes using dots or crosses. They could put each part on a part whole model too.	4+3=7 Four is a part, 3 is a part and the whole is seven.
Counting on using number lines using cubes or Numicon.	A bar model which encourages the children to count on, rather than count all.	The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? 4+2
Regrouping to make 10; using ten frames and counters/cubes or using Numicon. 6 + 5	Children to draw the ten frame and counters/cubes.	Children to develop an understanding of equality e.g. $6 + \Box = 11$ $6 + 5 = 5 + \Box$ $6 + 5 = \Box + 4$







Calculation Policy: Subtraction

Key Vocabulary - *take away, less than, the difference, subtract, minus, fewer, decrease.*

Concrete	Pictorial	Abstract
Physically taking away and removing objects from a whole (ten frames, Numicon, cubes and other items such as beanbags could be used).	Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.	4-3=
4 - 3 = 1	XXXX XXX	4 3 ? 4 ? 3
Counting back (using number lines or number tracks) children start with 6 and count back 2. 6 - 2 = 4 1 2 3 4 5 6 7 8 9 10	Children to represent what they see pictorially e.g.	Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line ///////////////////////////////////
Finding the difference (using cubes, Numicon or Cuisenaire rods, other objects can also be used). Calculate the difference between 8 and 5.	Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate.	Find the difference between 8 and 5. 8 – 5, the difference is Children to explore why 9 – 6 = 8 – 5 = 7 – 4 have the same difference.







Calculation Policy: Multiplication

Key Vocabulary - double, times, multiplied by, the product of, groups of, lots of, equal groups.





Partition to multiply using Numicon, base 10 or Cuisenaire rods. 4 × 15	Children to represent the concrete manipulatives pictorially.	Children to be encouraged to show the steps they have taken. 4×15 10 5 $10 \times 4 = 40$ $5 \times 4 = 20$ 40 + 20 = 60 A number line can also be used
Formal column method with place value counters (base 10 can also be used.) 3 × 23	Children to represent the counters pictorially. 10s 1s 00 000 00 000 00 000 6 9	Children to record what it is they are doing to show understanding. 3×23 $3 \times 20 = 60$ $3 \times 3 = 9$ 20 3 $60 + 9 = 6923\times 369$
Formal column method with place value counters. 6 x 23 100s 10s 1s 100s	Children to represent the counters/base 10, pictorially e.g. the image below.	Formal written method $6 \times 23 =$ 23 $\times 6$ 138 1 1 $1 \frac{24}{\times 26}$ $-\frac{7}{4} \frac{4}{4}$ $2 \frac{4}{\times 26}$ $-\frac{7}{4} \frac{4}{4}$ Answer: 3224



Calculation Policy: Division

Key Vocabulary - share, group, divide, divided by, half.













Conceptual Variation

Different representations of the same idea strengthens our understanding of what 'it' is.









